

Lecture 09Transformer based Object Detection

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- Transformer in NLP
- Multi-head Attention
- Vision transform (ViT)
- Swin-Transformer
- DETR
- RT-DETR
- Practice of RT-DETR

Transformer in NLP

- Transformer was first proposed by Google Brain in the domain of $NLP^{[1]}$
	- Transformer encoder is used to transform a set of tokens (vectors) $\mathcal I$ into another set of tokens \mathcal{O} , where each element in \mathcal{O} can catch the **global information** of \mathcal{I} ; usually the number of tokens in $\mathcal I$ and $\mathcal O$ are the same
	- This architecture has since become the foundation for many state-of-the-art NLP models, including BERT and GPT (Generative Pre-trained Transformer)
	- It is now also widely applied in computer vision
- Transformer encoder is composed of basic blocks, including **self-attention**, **positional encoding**, MLP, residual connection and **Layer-norm**
	- A set of vectors is transformed into another different set of vectors; that is why such ^a structure is called "transformer"

[1] VASWANI A, SHAZEER N, PARMAR N, et al. Attention is all you need[C]//Proc. Adv. Neural Inf. Process. Syst., 2017: 6000-6010. (**Cited by 125704**, Jun. 21, 2024)

Transformer in NLP

Ashish Vaswani (born in 1986) is ^a computer scientist. He was ^a co-founder of Adept AI Labs and ^a former staff research scientist at Google Brain. Vaswani completed his engineering in Computer Science from BIT Mesra (印度贝拉理工 学院,梅斯拉) in 2002. In 2004, he moved to the US to pursue higher studies at University of Southern California. He did his PhD at the University of Southern California.

The relationship among several terms, NLP, BERT, GPT, Transformer and self-attention

- It is the core componen^t in Transformer encoder
- Key characteristics of self-attention
	- Input *N* vectors with dimension *d*, output *N* vectors with dimension *d*
	- Each output vector can capture the **context information of all the input vectors**

Ex: word tagging for an input sentence "I saw ^a saw"

Naïve solution: deal with each word independently using ^a network

- \checkmark $W_{a} \in \mathbb{R}^{d \times d}, W_{b} \in \mathbb{R}^{d \times d}, W_{c} \in \mathbb{R}^{d \times d}$ are the matrices that need **to be learned by training** $\boldsymbol{W}_q \in \mathbb{R}^{d \times d}$, $\boldsymbol{W}_k \in \mathbb{R}^{d \times d}$, $\boldsymbol{W}_v \in \mathbb{R}^{d \times d}$ $\boldsymbol{W}_{\cdot}\in\mathbb{R}^{d\times d}$, $\boldsymbol{W}_{\cdot}\in\mathbb{R}^{d\times d}$, $\boldsymbol{W}_{\cdot}\in\mathbb{R}^{d\times d}$
- \checkmark q_1 is the **embedded query** vector
- \checkmark *k*₁, *k*₂, *k*₃, and *k*₄ are the **embedded** *key* vectors
- \mathbf{v}_1 , \mathbf{v}_2 , \mathbf{v}_3 , and \mathbf{v}_4 are the **embedded value** vectors

$$
\mathbf{q}_1 \in \mathbb{R}^{d \times 1}
$$
\n
$$
\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3, \mathbf{k}_4 \in \mathbb{R}^{d \times 1}
$$
\n
$$
\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3, \mathbf{v}_4 \in \mathbb{R}^{d \times 1}
$$

 $\alpha_{1,1} = k_1 \cdot q_1$ $_{1,2} - \cdots$ $_{2}$ $_{1}$ $_{1,3}$ – \mathbf{v}_3 – \mathbf{v}_1 $\alpha_{1,4} = k_4 \cdot q_1$ α α $=$ κ . $=$ K₂. = $k_{\gamma} \cdot q$ k ₃ \cdot q $\left(\alpha_{_{1,i}}\,/\,\sqrt{d}\,\right)$ $\left(\alpha_{\text{\tiny l},j}^{\text{}}\,/\,\sqrt{d}\, \right)$ $\sum_{1,i}^{\prime} = \frac{exp(\alpha_1)}{4}$ 1, 1 $\exp(\alpha_{\text{i}i}/\alpha_{\text{i}i})$ $\exp(\alpha_{\rm j}/\alpha_{\rm j})$ *i i j j d d* $\alpha_1 = \frac{\exp(\alpha_1)}{1}$ $\alpha_{\text{\tiny{l}}}$ = $=\frac{1}{\sum_{i=1}^{4}}$ softmax $\alpha_{\scriptscriptstyle 1,1}^{}$ 1,2 $\alpha_{1,3}$ $\alpha_{\scriptscriptstyle 1,4}^{}$ α α $\begin{pmatrix} \alpha_{\scriptscriptstyle 1,1}\ \alpha_{\scriptscriptstyle 1,2}\ \alpha_{\scriptscriptstyle 1,3}\ \alpha_{\scriptscriptstyle 1,4} \end{pmatrix}$ $\boldsymbol{\alpha}$ \triangleq attention scores softmax $\alpha^{'}_{1,1}$ α _{1,2} $\alpha_1 \triangleq$ $\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ 1,3 '1,4 α α α $\begin{pmatrix} \alpha_{1,1}^{\prime}\ \alpha_{1,2}^{\prime}\ \alpha_{1,3}^{\prime} \ \alpha_{1,4}^{\prime} \end{pmatrix}$ normalized attention scores

 \boldsymbol{b}_1 is the average of $\{\boldsymbol{v}_i\}$ weighted by $\boldsymbol{\alpha}_1^{\prime}$,

$$
\boldsymbol{b}_1 = \sum_{i=1}^4 \boldsymbol{\alpha}_{1,i}^{\mathbf{\prime}} \boldsymbol{v}_i = \left[\boldsymbol{v}_1 \ \boldsymbol{v}_2 \ \boldsymbol{v}_3 \ \boldsymbol{v}_4 \right] \boldsymbol{\alpha}_1^{\mathbf{\prime}}
$$

 b_2 ~ b_4 can be computed in the same way in parallel

 $\begin{split} \text{Let}~~~&I_{_{d\times 4}}\triangleq[\textit{\textbf{a}}_{_{1}}~\textit{\textbf{a}}_{_{2}}~\textit{\textbf{a}}_{_{3}}~\textit{\textbf{a}}_{_{4}}],~&\boldsymbol{Q}_{_{d\times 4}}\triangleq[\textit{\textbf{q}}_{_{1}}~\textit{\textbf{q}}_{_{2}}~\textit{\textbf{q}}_{_{3}}~\textit{\textbf{q}}_{_{4}}],~K_{_{d\times 4}}\triangleq[\textit{\textbf{k}}_{_{1}}~\textit{\textbf{k}}_{_{2}}~\textit{\textbf{k}}_{_{3}}~\textit{\textbf{k}}_{_{4}}],$ and $\boldsymbol{O}_{d\times 4}\triangleq[\boldsymbol{b}_{1}~\boldsymbol{b}_{2}~\boldsymbol{b}_{3}~\boldsymbol{b}_{4}]$

We have,
\n
$$
Q_{d\times d} = [q_1 q_2 q_3 q_4] = [W_q a_1 W_q a_2 W_q a_3 W_q a_4] = W_q I_{d\times 4}
$$
\n
$$
K_{d\times d} = [k_1 k_2 k_3 k_4] = [W_k a_1 W_k a_2 W_k a_3 W_k a_4] = W_k I_{d\times 4}
$$
\n
$$
V_{d\times 4} = [v_1 v_2 v_3 v_4] = [W_k a_1 W_k a_2 W_k a_3 W_k a_4] = W_v I_{d\times 4}
$$
\n
$$
\alpha_1 = \begin{pmatrix} \alpha_{1,1} = k_1 \cdot q_1 \\ \alpha_{1,2} = k_2 \cdot q_1 \\ \alpha_{1,3} = k_3 \cdot q_1 \\ \alpha_{1,4} = k_4 \cdot q_1 \end{pmatrix} = \begin{pmatrix} k_1^T q_1 \\ k_2^T q_1 \\ k_3^T q_1 \\ k_4^T q_1 \end{pmatrix} = K^T q_1 \qquad \alpha_2 = K^T q_2 \qquad \alpha_3 = K^T q_3 \qquad \alpha_4 = K^T q_4
$$
\n**softmax is applied to each column vector**
\n
$$
A_{4\times 4} = [\alpha_1 \alpha_2 \alpha_3 \alpha_4] = [K^T q_1 K^T q_2 K^T q_3 K^T q_4] = K^T [q_1 q_2 q_3 q_4] = K^T Q
$$
\n
$$
A_{4\times 4} = [\alpha_1 \alpha_2 \alpha_3 \alpha_4] = [\text{softmax}(\frac{\alpha_1}{\sqrt{d}}) \text{softmax}(\frac{\alpha_2}{\sqrt{d}}) \text{softmax}(\frac{\alpha_3}{\sqrt{d}}) \text{softmax}(\frac{\alpha_4}{\sqrt{d}})] = \text{softmax}(\frac{\alpha_4}{\sqrt{d}}) = \text{softmax}(\frac{A}{\sqrt{d}}) = \text{softmax}(\frac{K^T Q}{\sqrt{d}})
$$
\n
$$
Q = [b_1 b_2 b_3 b_4] = [V_{d\times 4} \alpha_1 V_{d\times 4} \alpha_2 V_{d\times 4} \alpha_3 V_{d\times 4} \alpha_4] = V_{d\times 4} [\alpha_1 \alpha_2 \alpha_3 \alpha_4] = V_{d\times 4}
$$

Multi-head Self-attention (MSA)

(single head) self-attention can be straightforwardly extend to multi-head self-attention

Positional encoding

•Can the self-attention really solve our word-tagging problem?

- \checkmark Using the self-attention, actually \bm{b}_2 and \bm{b}_4 are the same!
- Accordingly, the two "saw"s will be predicted to have the same tagging

What do we miss?

The position information of the vectors in the input sequence

That the two "saw"s have different tagging largely owes to the fact that they have different positions in the sequence

We need to modify the input vectors by embedding their positional information

Positional encoding

For each input vector $a_t \in \mathbb{R}^{d \times 1}$, construct a positional encoding vector $pe_t \triangleq \left\{pe_t^{(i)}\right\}_{i=0}^{d-1}$

$$
pe_i^{(i)} = \begin{cases} \sin(w_k t), & \text{if } i = 2k \\ \cos(w_k t), & \text{if } i = 2k + 1 \end{cases}
$$

where *t* is the position of this input vector in the sequence, $w_k = \frac{1}{100002k/d}$, $k=0, 1$, 2,…, *d*/2-1 1 $W_k = \frac{10000^{2k/d}}{10000^{2k/d}}$

Positional encoding means that we modify a_t as a_t + pe_t

with positional encoding

Layer-norm VS batch-norm

- • Batch-norm and layer-norm are two strategies for training neural networks faster and more stably
- • In Yolov3, we have met batch-norm; in transformer-related structures, in most cases, they use layer-norm
- \bullet Batch-norm VS layer-norm
	- Batch-norm normalizes each feature (channel) independently across the samples in a mini**batch**
	- Layer-norm normalizes each sample in the mini-batch independently across all features **(channels)**
	- As batch-norm is dependent on batch size, it's not effective for small batch sizes

Layer-norm VS batch-norm

They use the same updating formular, but adopt different ways to compute statistics (μ, σ^2) ,

$$
y_i \leftarrow \gamma \frac{x_i - \mu}{\sqrt{\sigma^2 + \varepsilon}} + \beta
$$

where *γ* and *β* are learnable parameters; for batch-norm, each neuron (channel) has ^a (*γ*, *β*) pair while for layer-norm each layer has ^a (*γ*, *β*) pair

- \checkmark C means the feature channels, $H \times W$ defines the instances of ^a feature by ^a sample, and *N* means the number of samples in ^a mini-batch
- \checkmark The normalization is applied to the blue part

For our case, *C*= *d*, *H*×*W=*4, *N*=1

Transformer encoder

- \checkmark The inputs are embedded in a sequence of vectors with the same length
- \checkmark Then, the embedded vectors are modified with positional encoding
- \checkmark Transformer encoder is composed of *N* blocks with the same structures
- \checkmark Each block processes the input vectors by a multi-head self-attention layer, ^a residual connection layer, ^a layernorm operation, ^a vector-wise fully connected MLP, another residual connection layer, and another layernorm
- If the dimension of the input is $d \times N$, the output of a transformer encoder will also be *d*×*N*

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Multi-head Attention

Self-attention

Let
$$
I_{d \times 4} \triangleq [a_1 a_2 a_3 a_4], Q_{d \times 4} \triangleq [q_1 q_2 q_3 q_4], K_{d \times 4} \triangleq [k_1 k_2 k_3 k_4], V_{d \times 4} \triangleq [v_1 v_2 v_3 v_4], A_{d \times 4} \triangleq [\alpha_1 \alpha_2 \alpha_3 \alpha_4], A_{d \times 4} \triangleq [\alpha_1' \alpha_2' \alpha_3' \alpha_4']
$$

\nand $Q_{d \times 4} \triangleq [b_1 b_2 b_3 b_4]$
\nWe have,
\n $Q_{d \times 4} = [q_1 q_2 q_3 q_4] = [W_q a_1 W_q a_2 W_q a_3 W_q a_4] = W_q I_{d \times 4}$
\n $K_{d \times 4} = [k_1 k_2 k_3 k_4] = [W_k a_1 W_k a_2 W_k a_3 W_k a_4] = W_k I_{d \times 4}$
\n $V_{d \times 4} = [v_1 v_2 v_3 v_4] = [W_v a_1 W_v a_2 W_v a_3 W_v a_4] = W_v I_{d \times 4}$
\nvalue sequence

In self-attention, the query sequence, the key sequence and the value sequence are actually identical; that is why it is called **self**-attention.

If the key sequence and the value sequence are the same while the query sequence is different, the self-attention changes to **attention**. In other words, self-attention is ^a special case of attention

Multi-head Attention

- • Multi-head attention is an extension to the multi-head self-attention; their computation frameworks are the same, excep^t that **in multi-head attention, the query sequence is different from the key and value sequences**
- •Multi-head attention can be used in **transformer decoders**

A multi-head attention module with *M* heads can be expressed as ^a function mh-attn,

$$
I_q \in \mathbb{R}^{d \times N_q}
$$
 is the query sequence; $I_{kv} \in \mathbb{R}^{d \times N_{kv}}$ is the key/value sequence
\n
$$
W \in \mathbb{R}^{d \times d \times 3 \times M}
$$
 is the weight tensor, where $d' = \frac{d}{M}$ is the dimension of the embedded vectors in each single-head
\n
$$
W_c \in \mathbb{R}^{d \times d \times 3 \times M}
$$
 is the original time, where $d' = \frac{d}{M}$ is the dimension of the embedded vectors in each single-head
\n
$$
W_c \in \mathbb{R}^{d \times d}
$$
 is the final output
\n
$$
Q \in \mathbb{R}^{d \times d'}
$$
 is the final output
\nRemember: each query generates an output vector

Multi-head Attention

Multi-head attention

$$
\min\left(\underbrace{I_q}_{d\times N_q}, \underbrace{I_{kv}}_{d\times N_{kv}}, \underbrace{W}_{d\times d\times 3\times M}, \underbrace{W_o}_{d\times d}\right): \mapsto \underbrace{Q}_{d\times N_q}
$$

Similar as multi-head self-attention, the final output of ^a MHA module is generated by

- \checkmark Concatenating the outputs of all the single-heads
- \checkmark then perform a linear mapping using W _o

 $\bm{O}_{d\times N_q}^{'}\!=\!\!\left[\, \text{attn}\!\left(\bm{I}_q^{},\bm{I}_k^{},\bm{W}_1^{}\right)\!; \text{attn}\!\left(\bm{I}_q^{},\bm{I}_k^{},\bm{W}_2^{}\right)\!; \!\cdots\!; \text{attn}\!\left(\bm{I}_q^{},\bm{I}_k^{},\bm{W}_M^{}\right)\right]$ ' $\bm{O}_{d\times N_q} = \bm{W}_o \bm{O}_{d\times N_q}$

where $\text{attn}\left(\mathbf{I}_q, \mathbf{I}_k, \mathbf{W}_h\right) \in \mathbb{R}^{d \times N_q}$ is the output of the h^{th} single-head and $W_{\mu} \in \mathbb{R}^{d^2 \times d \times 3}$ is the *h*th "slice" of the tensor*W*; [;] denotes the channel-wise concatenation *h* $W_{i} \in \mathbb{R}^{d \times d \times d}$

$Single-head$

$$
\text{attn}\left(\boldsymbol{I}_q,\boldsymbol{I}_{kv},\boldsymbol{W}\right)\in\mathbb{R}^{d^{\prime}\times N_q}
$$

where $W = [W_1; W_2; W_3] \in \mathbb{R}^{d' \times d \times 3}$ is the weight tensor for this head; $W_1 \in \mathbb{R}^{d' \times d}$, $W_2 \in \mathbb{R}^{d' \times d}$, $W_3 \in \mathbb{R}^{d' \times d}$ are used to compute embedded queries, keys, and values, respectively **Positional encoding** $\boldsymbol{W}_1 \in \mathbb{R}^{d' \times d}$, $\boldsymbol{W}_2 \in \mathbb{R}^{d'}$ $\mathbf{W}_2 \in \mathbb{R}^{d' \times d}$, $\mathbf{W}_3 \in \mathbb{R}^{d'}$ $W_2 \in \mathbb{R}^{d \times d}$ $\bm{\mathcal{Q}}_{d^{'}\times N_{q}}^{\mathstrut} \! = \! \bm{W}_{\!1}^{\text{'}}\! \left(\bm{I}_{q}^{\mathstrut} \! + \! \bm{P}_{\!q}^{\mathstrut} \right)\!, \bm{K}_{d^{'}\!\times\! N_{k\!v}}^{\mathstrut} \! = \! \bm{W}_{\!2}^{\text{'}}\! \left(\bm{I}_{k\!v}^{\mathstrut} \! + \! \bm{P}_{\!k\!v}^{\mathstrut} \right)\!,\! \bm{\mathit{V}}_{d^{'}\!\times\! N_{k\!v}}^{\mathstrut} \! = \! \bm{W}_{\!$

 $\overline{}$ Compute the normalized attention scores between *qⁱ*and *K*,

$$
\boldsymbol{\alpha}_{i} \triangleq (\boldsymbol{\alpha}_{i,1}, \boldsymbol{\alpha}_{i,2},..., \boldsymbol{\alpha}_{i,N_{kv}})^{T}, \quad \boldsymbol{\alpha}_{i,j} = \frac{\exp(k_{j}^{T}\boldsymbol{q}_{i} / \sqrt{d}^{T})}{\sum_{k=1}^{N_{kv}} \exp(k_{k}^{T}\boldsymbol{q}_{i} / \sqrt{d}^{T})}
$$

The *i*-th output vector of this head is,

$$
\text{attn}_{i}\left(\boldsymbol{I}_{q}, \boldsymbol{I}_{kv}, \boldsymbol{W}^{'}\right) = \sum_{j=1}^{N_{kv}} \boldsymbol{\alpha}_{ij} \boldsymbol{v}_{j} = \boldsymbol{V} \boldsymbol{\alpha}_{i} \in \mathbb{R}^{d^{'} \times 1}
$$

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- • Inspired by the grea^t success of transformer in the field of NLP, researchers in CV have started to adopt transformers in CV tasks
- The first image classification framework totally based on transformer is ViT (Vision Transformer) proposed also by researchers of Google in 2021

Alexey Dosovitskiy received the M.Sc. and Ph.D. degrees in mathematics (functional analysis) from Moscow State University, Moscow, Russia, in 2009 and 2012, respectively.,He is currently ^a Research Scientist with the Intelligent Systems Laboratory, Intel, Munich, Germany. From 2013 to 2016, he was ^a Postdoctoral Researcher, with Prof. T. Brox, with the Computer Vision Group, University of Freiburg, Breisgau, Germany, working on various topics in deep learning, including self-supervised learning, image generation with neural networks, motion, and 3-D structure estimation.

[1] DOSOVITSKIY A, BEYER L, KOLESNIKOV A, et al. An image is worth 16x16 words: Transformers for image recognition at scale[C]//Proc. Int'l. Conf. Learning Representations, 2021. (**Cited by 38008**, Jun. 25, 2024)

视觉Transformer

视觉Transformer

 \checkmark A learnable vector a_0 is added here and is expected to hold the global information of the image for classification; a_0 can be randomly initialized

With a_0 , the input vectors can be seen as ^a matrix,

 $A \triangleq [a_0 a_1 a_2 ... a_9] \in \mathbb{R}^{1024 \times 10}$

For positional encoding, ViT uses ^a learnable matrix *PE* ∈ $\mathbb{R}^{1024 \times 10}$

Then, the input vectors with positional encoding form the matrix

 $A + PE \in \mathbb{R}^{1024 \times 10}$

视觉Transformer

 \checkmark **b**₀ corresponds to a_0 ; as it is the output of ^a transformer encoder, it can hold the global information of all the block vectors and can be trained toperform the classification task

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- ViT is ^a cool idea and demonstrates that transformer has ^a good potential in CV; however, it has too many parameters and thus is computationally expensive
- \bullet Swin-Transformer^[1] proposes several universal and straightforward ideas to improve ViT
	- To reduce computational cost: **self-attention is restricted to ^a local window**
	- To make the outputs of the self-attention still capture the contextual information: **windows** used to compute self-attention are shifted and the self-attention is repeated; the shifted window partitioning approach introduces connections between neighbhoring nonoverlapping windows in the previous layer
	- To ge^t multi-resolution feature maps (as Yolov3 and Yolov8): **^a patch merging mechanism is proposed**; the obtained hierarchical representation is very similar to multiresolution CNN feature maps

[1] LIU Z, LIN Y, CAO Y, et al. Swin transformer: Hierarchical vision transformer using shifted windows[C]//Proc. IEEE Int'l. Conf. Computer Vision, 2021: 9992-10002. (**Cited by 19016**, July 4, 2024)

Marr Prize

Swin Transformer: Hierarchical Vision Transformer using Shifted Windows

Ze Liu (USTC), Yutong Lin (Xi'an Jiaotong University), Yue Cao (Microsoft Research), Han Hu (Microsoft Research Asia), Yixuan Wei (Tsinghua University), Zheng Zhang (MSRA, Huazhong University of Science and Technolog), Stephen Lin (Microsoft Research), Baining Guo (MSR Asia)

Session 8 (A/B)

Ze Liu is currently ^a final-year joint Ph.D. candidate at the University of Science and Technology of China (USTC) and Microsoft Research Asia (MSRA)

- \checkmark Two swin-transformer encoders are used in pair
- \checkmark With respect to structures, they are similar to the transformer encoder of ViT; the only difference is that the swin-transformer encoders compute multi-head self-attention in local windows
- \checkmark The windows used in SW-MSA are shifted from windows in W-MSA; the window-shifting mechanism can supplement connections across non-overlapping windows

Window-partition in W-MSA Window-partition in SW-MSA

Swin-Transformer Encoders **Note: Each point actually is a vector**

How to perform positional encoding?

Using ^a common positional encoding strategy,

- \checkmark PE matrix can be pre-fixed (such as sinusoid functions) or can be learned as in the case of ViT
- \checkmark Such a positional encoding strategy can be considered as a "1-D" strategy since the vectors are arranged in a line
- **The "2D" positional relationships of the vectors cannot be well embedded in such a way Relative Position Bias**

• Relative position bias can encode the relative position relationship between two vectors in ^a 2D array

E.g., the RPB of "2" to "1" is the same as the RPB of "4" to "3"

• Positional encodings are added to the input vectors; differently, RPBs are added to attention scores

Embedded queries and keys: $Q \in \mathbb{R}^{d \times m^2}$, $K \in \mathbb{R}^{d \times m^2}$ Attention scores,

$$
A_{m^2 \times m^2} = \mathbf{K}^T \mathbf{Q} = \begin{bmatrix} \alpha_{1,1} & \alpha_{2,1} & \cdots & \alpha_{m^2,1} \\ \alpha_{1,2} & \alpha_{2,2} & \cdots & \alpha_{m^2,2} \\ \vdots & \vdots & & \vdots \\ \alpha_{1,m^2} & \alpha_{2,m^2} & \cdots & \alpha_{m^2,m^2} \end{bmatrix}
$$

It implies that the RPB matrix *B* should be of the dimension $m^2 \times m^2$, and $B(i, j)$ reflects the relative position of the query *qⁱ* and the key *^k^j*

• Relative position bias can encode the relative position relationship between two vectors in ^a 2D array

E.g., the RPB of "2" to "1" is the same as the RPB of "4" to "3"

• Positional encodings are added to the input vectors; differently, RPBs are added to attention scores

$$
A'_{m^{2} \times m^{2}} = softmax \left(\frac{K^{T} Q}{\sqrt{d}} + B \right)
$$

= softmax $\left(\frac{1}{\alpha_{1,1}} \begin{array}{ccc} 2 & 3 & 4 \\ \hline \alpha_{2,1} & \alpha_{3,1} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.7 \\ \hline \alpha_{1,2} & \alpha_{2,2} & \alpha_{3,1} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.7 \\ \hline \alpha_{1,2} & \alpha_{2,2} & \alpha_{3,2} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.7 \\ \hline \alpha_{1,3} & \alpha_{2,3} & \alpha_{3,3} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.7 \\ \hline \alpha_{1,4} & \alpha_{2,4} & \alpha_{3,4} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.8 \\ \hline \alpha_{1,4} & \alpha_{2,4} & \alpha_{3,4} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.2 \\ \hline \alpha_{1,4} & \alpha_{1,4} & \alpha_{1,4} \end{array} \begin{array}{ccc} 4 & 0.4 & 0.8 & 0.7 \\ \hline \alpha_{1,4} & \alpha_{1,4} & \alpha_{1,4} \end{array} \right)$

- \checkmark Half the spatial resolution
- \checkmark Double the channels

- • Play with Swin-Transformer
	- Swin-Transformer is ^a backbone network architecture
	- It outputs 4 feature maps with four different spatial resolutions; these four feature maps can be used similar as CNN feature maps; thus with different task heads, it can be used for object detection, object classification, semantic segmentation, etc.

The authors provide pre-trained Swin-Transformer models at four different scales

| | downsp. rate (output size) | $Swin-T$ | Swin-S | Swin-B | Swin-L |
|---------|--------------------------------|--|--|---|--|
| stage 1 | $4\times$ (56×56) | concat 4×4 , 96-d, LN | concat 4×4 , 96-d, LN | concat 4×4 , 128-d, LN | concat 4×4 , 192-d, LN |
| | | win. sz. 7×7 , $\times 2$ $dim 96$, head 3 | win. sz. 7×7 , $\times 2$ $dim 96$, head 3 | win. sz. 7×7 , $\times 2$ dim 128, head 4 | win. sz. 7×7 , $\times 2$ dim 192, head 6 |
| stage 2 | $8\times$ (28×28) | concat 2×2 , 192-d, LN | concat 2×2 , 192-d, LN | concat 2×2 , 256-d, LN | concat 2×2 , 384-d, LN |
| | | win. sz. 7×7 , $\times 2$ dim 192, head 6 | win. sz. 7×7 , $\times 2$ dim 192, head 6 | win. sz. 7×7 , $\times 2$ $dim 256$, head 8 | win. sz. 7×7 , $\times 2$ dim 384, head 12 |
| stage 3 | $16\times$ (14×14) | concat 2×2 , 384-d, LN | concat 2×2 , 384-d, LN | concat 2×2 , 512-d, LN | concat 2×2 , 768-d, LN |
| | | win. sz. 7×7 , \times 6 dim 384, head 12 | win. sz. 7×7 , $\times 18$ dim 384, head 12 | win. sz. 7×7 , $\times 18$ dim 512, head 16 | win. sz. 7×7 , $\times 18$ dim 768, head 24 |
| stage 4 | $32\times$ (7×7) | concat 2×2 , 768-d, LN | concat 2×2 , 768-d, LN | concat 2×2 , 1024-d, LN | concat 2×2 , 1536-d, LN |
| | | win. sz. 7×7 , $\times 2$ dim 768, head 24 | win. sz. 7×7 , $\times 2$ dim 768, head 24 | win. sz. 7×7 , $\times 2$ dim 1024, head 32 | win. sz. 7×7 , \times 2 dim 1536, head 48 |

Outline

- Transformer in NLP
- Multi-head Attention
- Vision transform (ViT)
- Swin-Transformer
- DETR
- RT-DETR
- Practice of RT-DETR

